

1. The abscissa of a particle is given by $x(t) = bt(1 - ct)$, where $b=3$, $c=0,25$ (in SI). Find:
 - a) Measurement units for b and c .
 - b) The velocity and the acceleration of the particle.
 - c) The time until the particle returns to the origin.

2. A body moves according to the equation $x(t) = ae^{-\beta t} \sin \omega t$, where $\beta, \omega > 0$ are constant.). Find:
 - a) Measurement units for β and ω .
 - b) The velocity and the acceleration of the particle for $t=0$.
 - c) The moments when the body attains extreme positions.

3. A body moves in the positive Ox axis, its velocity varying according to the law $v(t) = b\left(1 - \frac{t}{c}\right)$, where $b=10$, $c=5$ (in SI). Find:
 - a) Measurement units for b and c .
 - b) The coordinate $x(t)$. Its values at $t=5$ s and $t=10$ s.
 - c) Moments at which $x(t)=9$ m.

4. The position of a body is given by $x(t) = ae^{-t/\tau} \cos(\omega t + \alpha)$. Compute the constants a and α in two situations:
 - a) Initial conditions are $x(0) = 0, v(0) = v_0$
 - b) Initial conditions are $x(0) = x_0, v(0) = 0$

5. A particle moves along the Ox axis according to the law: $x(t) = A \cos \frac{2\pi}{T} t$. Find:
 - a) The velocity and the acceleration of the body.
 - b) The distance traveled by the body during the time interval from $t=0$ to $t=T/8$.
 - c) The distance traveled in the time interval T .

6. The components of a particle's velocity are:

$$v_x = A \sin \omega t, \quad v_y = A \sin \left(\omega t + \frac{\pi}{2} \right), \quad v_z = 0.$$
 Find the modulus of the velocity, the acceleration and its modulus, as well as the angle between \vec{v} and \vec{a} . Discuss.

7. The time dependence of the coordinate of a particle is given by:

$$x = A \sin \omega t, \quad y = A \sin \left(\omega t + \frac{\pi}{2} \right), \quad z = 0.$$
 Compute the position vector \vec{r} , the velocity \vec{v} and the acceleration \vec{a} . Compute the angles between \vec{r} and \vec{v} and between \vec{r} and \vec{a} . Discuss.

8. A particle is thrown from the origin of the frame xOy at the moment $t=0$, with velocity v_0 at a certain angle θ from the Ox axis. At the same moment another particle begins to fall freely from a wall with height h , situated at the distance d . Air resistance is neglected. Find the angle θ in order that the two bodies meet. What condition must satisfy the initial velocity v_0 ?

9. The potential energy of a particle is given by $U = \frac{kx^2}{2}$. Find the force acting on the particle and the work W done on it when the body moves from the point $A(1, 1, 2)$ to the point $B(2, 1, 2)$.
10. A pendulum of length $l = 1\text{ m}$ and mass $m = 2\text{ kg}$ moves in a vertical plane, the maximum deviation angle being $\alpha = 30^\circ$. Find:
- The kinetic and potential energies of the body during the movement.
 - The angular momentum of the body measured with respect to the hook.