

Related Topics

Refractive index, wavelength, frequency, phase, modulation, heterodyne technique, electric field constant, magnetic field constant.

Principle

The intensity of a laser diode is modulated with a high frequency and the beam is reflected, after traveling some distance, back into the apparatus. The phase of the received signal is compared to the one transmitted. The velocity of light is then calculated from the measured phase difference, the modulation frequency and the length of the light path.

Equipment

1 Speed of Light meter (complete set)	11226-88
2 Screened cable, BNC, l = 750 mm	07542-11
1 Digital Oscilloscope 25 MHz, 2 channels	11456-99

Tasks

1. Determine the velocity of light in air.
2. Determine the velocity of light in water and calculate the refractive index.
3. Determine the velocity of light in acrylic glass and calculate the refractive index.

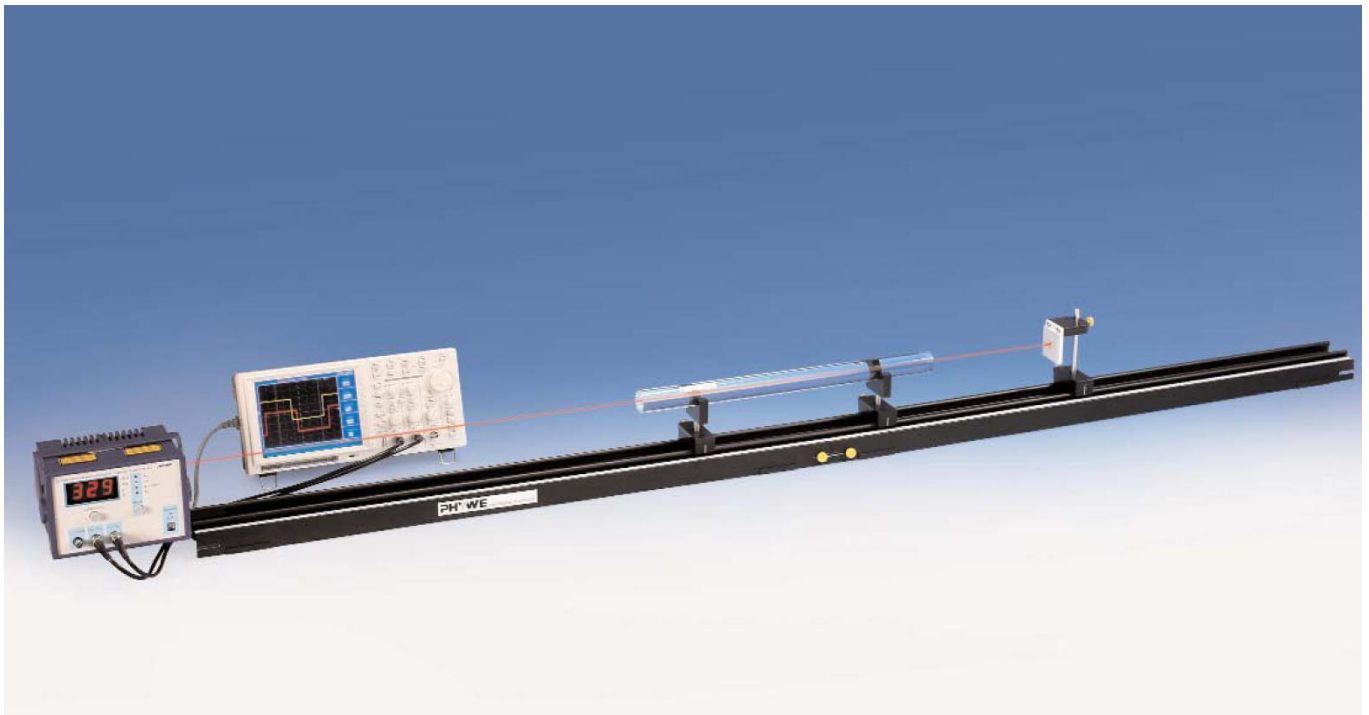


Fig. 1: Set-up of experiment

Set-up and Procedure

The light velocity measuring apparatus and the mirror are set up in such a way that the laser beam hits the mirror no matter where along the base the mirror is placed (more detailed directions can be found in the operating instructions of the Speed of Light meter). First the socket $f_{\text{emmit}}/1000$ is connected to the oscilloscope and the modulation frequency f_{emmit} (divided by 1000) is determined. The reason for introducing the fixed factor $1/1000$ into the hardware between the modulator and the socket, is that a relatively simple oscilloscope can be used for the task.

After determination of the modulation frequency, the two other sockets ($f_{\text{emmit}} - f_{\text{sync}}$ and $f_{\text{rec}} - f_{\text{sync}}$) are connected to the two input sockets of the oscilloscope. The frequencies of the emitted and the received signal are also reduced to 50 KHz while conserving their phase relation so that they can be displayed on this type of oscilloscope.

Task 1: The velocity of light in air

At the start the mirror is placed close to the operating unit, the mode " $\Delta\varphi$ " is selected and the button "Calibration" is pressed to have two coinciding signals visible on the oscilloscope. (See Fig. 2)

The mirror is then slid along the graduated scale. For at least 10 different displacements Δx (> 100 cm) the time difference Δt is calculated from the readings performed on the oscilloscope. (See Fig. 3).

Task 2: The Velocity of light in water and Task 3: The Velocity of light in acrylic glass

The water-filled tube or the acrylic glass rod is placed so that the laser beam runs through them, the mirror is placed directly behind. The "Calibration" button is pressed. Again the oscilloscope will show a graph similar to Fig. 2. The tube/rod is then taken out of the path of the rays, the two signals will not coincide any longer. Now the mirror is moved a distance Δx until the two signals on the oscilloscope coincide again as before with the medium inserted. The mirror displacement Δx is measured several times.

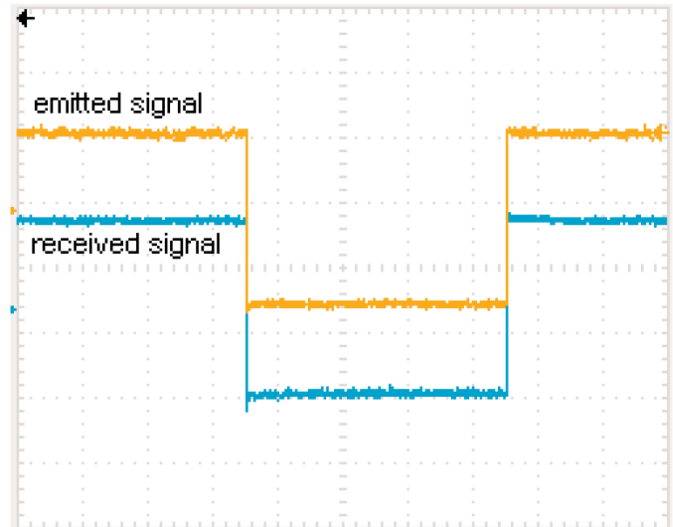


Fig. 2. Oscilloscope signal after "Calibration".

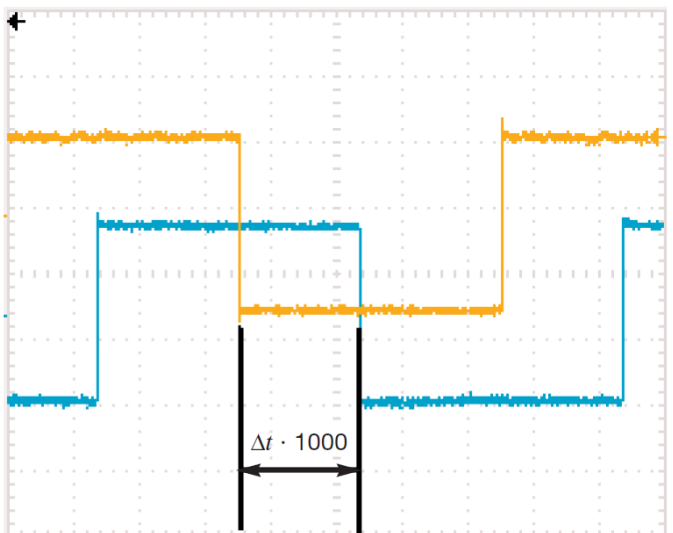


Fig. 3. Measuring the time difference using the oscilloscope.

Theory and evaluation

Although light travels very fast, its velocity is finite. Since 1676 when Romer estimated the velocity of light using spatial scales that included the distances to the moons of Jupiter much technical development took place. These days we can comfortably measure the speed of light on a table top. In the SI system, the metre is defined as the distance light travels in vacuum in $1/299792458$ of a second. The effect of this definition is to fix the speed of light in vacuum at exactly

299 792 458 m/s.

Velocity of light in air:

To obtain the velocity of light, one has calculate $\Delta t/\Delta s$. Where Δt is the time the light takes to travel the distance Δs . The distance Δs is $2 \cdot \Delta x$ because the additional stretch is twice the mirror displacement since the laser beam has to travel to the mirror and back again.

Table 1 gives an example of a measurement:

Δx in mm	Δs in mm	Δt in ns	$c = \Delta s/\Delta t$ in (m/s · 10 ⁸)
1000	2000	6.6	3.03
1100	2200	7.3	3.01
1200	2400	7.9	3.03
1300	2600	8.6	3.02
1350	2700	9.0	3.00
1400	2800	9.3	3.01
1450	2900	9.6	3.02
1500	3000	9.9	3.03
1550	3100	10.3	3.01
1600	3200	10.6	3.02
			av. val.: 3.018

Velocity of light in water/acrylic glass

The velocity of light in water or acrylic glass, c_m , is measured by comparing it with the velocity of light in air c_a (Fig. 4). In the first measurement (with the medium), the light travels a distance l_1 in time t_1 ($l_1 = 2x1$).

In the second measurement (no medium), the light travels a distance $l_2 = l_1 + 2\Delta x$ in the same time. This

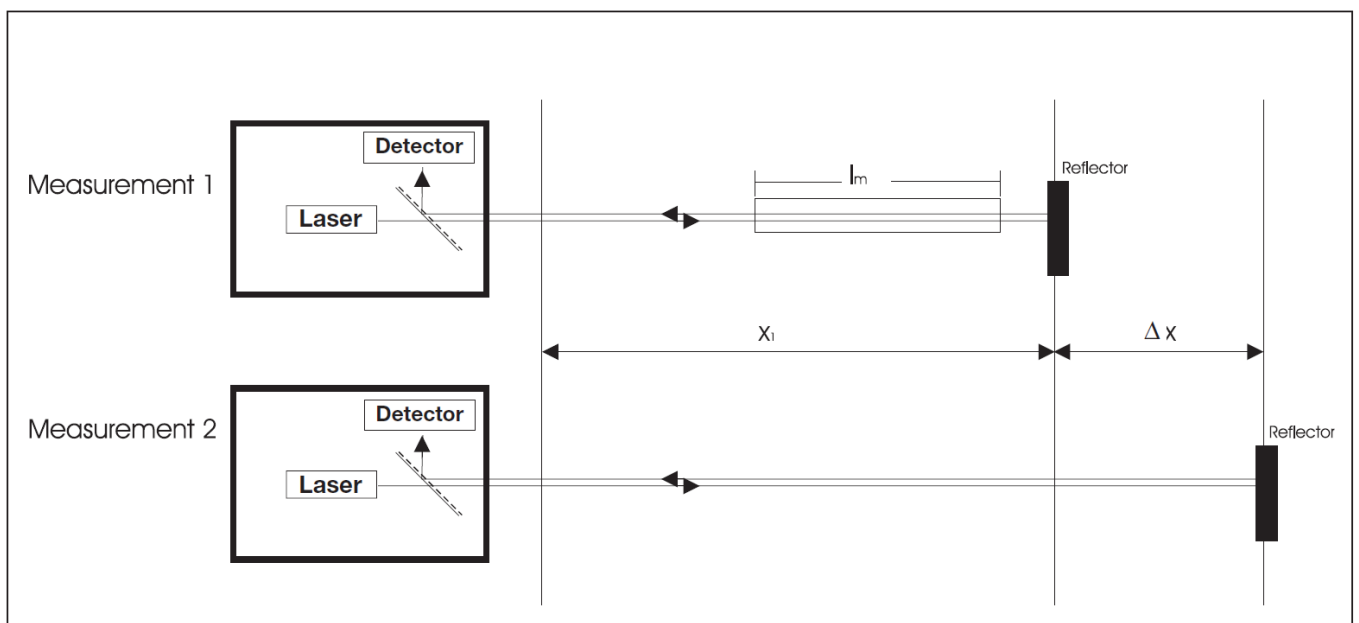


Fig. 4: Principle for measuring the velocity of light in a medium

means that light takes the same time to travel the distance $2\Delta x + 2l_m$ in air as it takes to travel the distance $2l_m$ in the medium.

From this and the definition of the refractive index, it follows directly, that

$$n_m = \frac{(2\Delta x + 2l_m)}{2l_m} = \frac{(\Delta x + l_m)}{l_m}$$

and

$$c_m = \frac{c_a}{n_m}$$

For the water-filled tube, with $l_m = 500$ mm as the length of the water column and a measured Δx of 170 mm, this leads to:

$$n = 1.34, \text{ (literature value: } n_{\text{water}} = 1.33)$$

$$c_{\text{water}} = 2.23 \cdot 10^8 \text{ m/s}$$

For the acrylic glass cylinder, with $l_m = 490$ mm and $\Delta x = 240$ mm:

$$n = 1.49, \text{ (literature values are in the range from: } n = 1.48 \text{ to } n = 1.52)$$

$$c_{\text{acrylic glass}} = 2.01 \cdot 10^8 \text{ m/s}$$

Note

The evaluation as described here relies completely on the measurements performed with the oscilloscope. No use is made of the displayed values on the velocity of light apparatus.

The reasons for this are mainly didactical ones: The students learn to operate an oscilloscope and they will trust the results more if they measured them themselves this way instead of taking the reading off an apparatus that is made just for this specific measurement. Nevertheless, in many settings (e.g. demonstration in class) it might be quite helpful to use the features built into the apparatus that are described in the manual.